

**UNIVERSITI SAINS MALAYSIA**

**Peperiksaan Semester Tambahan**

**Sidang Akademik 1992/93**

**Jun 1993**

**FMT 202 Statistik**

**Masa: (2 jam)**

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Kertas ini mengandungi ENAM (6) soalan.

Jawab LIMA (5) soalan sahaja.

Semua soalan mesti dijawab dalam Bahasa Malaysia

...2/-

1. (A) Diberikan nombor-nombor berikut:

4, 6, 12, 4, 10, 12, 3, x, y

mean untuk nombor tersebut ialah 7, mod ialah 4,

Tentukan (i) nilai-nilai untuk x dan y

(ii) median untuk 9 nombor tersebut

- (B) Sekiranya dua nombor  $(7+m)$  dan  $(7-m)$  ditambahkan lagi ke 9 nombor tadi, sisihan piawai untuk 11 nombor itu ialah 4.

Tentukan (i) mean untuk 11 nombor

(ii) nilai m

(20 markah)

2. IQ untuk 500 orang pelajar ditunjukkan di dalam jadual berikut:

IQ	Bil. Pelajar	IQ	Bil. Pelajar
82-85	5	106-109	75
86-89	19	110-113	56
90-93	32	114-117	39
94-97	49	118-121	28
98-101	71	122-125	18
102-105	92	126-129	10
		130-133	6

...3/-

Gunakan kaedah pengkodan untuk mencari:

- (i) mean
- (ii) sisihan piawai
- (iii) median
- (iv) bilangan pelajar yang mempunyai IQ di antara  $\pm$  satu sisihan piawai daripada mean.

Catatan: nilai  $u_i$  tidak boleh melebihi  $\pm 10$ .

(20 markah)

3. (A) Satu penyelidikan telah dijalankan untuk mengkaji paras klorida urin di dalam individu normal dan pesakit hipertensi. Adalah diandaikan paras klorida urin individu normal ialah 200 mEq/24 jam dan sisihan piawainya ialah 15 mEq/24 jam. Paras klorida urin di dalam pesakit hipertensi ialah 160 mEq/24 jam. Berasaskan data yang diberi, tentukan sama ada pesakit hipertensi mempunyai paras klorida urin yang lebih rendah daripada individu normal?  
(gunakan  $\alpha = 0.01$ ).

(10 markah)

- (B) Tentukan selang keyakinan di peringkat 99 peratus, min paras klorida urin pesakit hipertensi.

(10 markah)

...4/

4. (A) Sekumpulan 50 penagih dadah telah didedahkan kepada dua jenis rawatan pemulihan. 25 orang daripada mereka telah menerima rawatan perubatan tradisional dan bakinya telah dirawat dengan drug nalokson. 16 orang daripada kumpulan yang menerima rawatan perubatan tradisional dan 11 orang daripada kumpulan yang menerima nalokson telah didapati pulih. Tentukan sama ada pemulihan daripada ketagihan berbeza atau tidak di antara kumpulan yang menerima rawatan perubatan tradisional dan kumpulan yang menerima nalokson di peringkat 95%.

(15 markah)

- (B) Bincangkan prinsip-prinsip rekabentuk ujikaji yang baik.

(5 markah)

5. Kandungan drug X dalam tablet yang dikeluarkan oleh dua kilang yang berbeza dibandingkan. Untuk tujuan ini 6 tablet dari setiap kilang itu diambil dan kandungan drugnya disukatkan. Berikut ialah keputusan yang diperolehi.

...5/-

Kandungan drug X (mg)	
Kilang No. 1	Kilang No. 2
7.1	9.5
7.9	9.8
8.6	10.2
6.8	11.3
9.6	11.4
9.2	10.8

- (A) Gunakan suatu ujian statistik yang sesuai untuk menentukan sama ada kandungan drug X dalam tablet yang dikeluarkan oleh dua kilang itu adalah berbeza secara statistik atau tidak.

(12 markah)

- (B) Apakah andaian-andaian anda buat apabila menggunakan ujian statistik yang anda pilih itu?

(4 markah)

- (C) Dari segi keseragaman kandungan, tablet dari kilang yang mana adalah lebih baik?

(4 markah)

...6/-

6. Berikut ialah data berat badan dan kepekatan kolesterol dalam darah yang diperolehi dari 8 orang manusia.

<u>Berat badan (kg)</u>	<u>Kepekatan kolesterol (<math>\mu\text{mol/L}</math>)</u>
58	151
45	141
67	162
75	196
78	199
80	213
85	226
90	237

- (A) Tentukan sama ada perhubungan di antara berat badan dan paras kolesterol itu adalah signifikan secara statistik atau tidak.

(10 markah)

- (B) Dua kaedah analisis yang digunakan untuk menentukan paras suatu drug Y dalam darah dibandingkan. Terangkan bagaimana anda akan mengendalikan perbandingan itu?

(10 markah)

...7/-

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FORMULA

$$1. \text{ Median } (m) = b + c \times \frac{d}{f}$$

$$2. u_i = Ax_i + B$$

$$3. \bar{x} = \frac{1}{A} (\bar{u} - B)$$

$$4. S_x^2 = \frac{1}{A^2} S_u^2$$

$$5. S_u^2 = \frac{\sum u_i^2 f_i - n\bar{u}^2}{n - 1}$$

$$6. \text{ Trimean} = \frac{\text{kuartil atas} + (2 \times \text{median}) + \text{kuartil bawah}}{4}$$

7. Ujian-t

$$t = \frac{\bar{x} - \mu_0}{S/\sqrt{n}}$$

$$s = \sqrt{\frac{x^2 - \frac{(\sum x)^2}{n}}{n - 1}}$$

$$t = \frac{\bar{x}_1 - \bar{x}_2}{S\sqrt{1/n_1 + 1/n_2}}$$

$$s = \sqrt{\frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}}$$

$$t = \frac{\bar{D}}{S/\sqrt{n}}$$

$$s = \sqrt{\frac{\sum D^2 - \frac{(\sum D)^2}{n}}{n - 1}}$$

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8. Ujian Wilcoxon (independent samples)

$$U = n_1 n_2 + \frac{n_2(n_2 + 1)}{2} - \Sigma R$$

$$U' = n_1 n_2 - U$$

9. Ujian Sign

$$P(s \geq k) = 1 - P(s \leq k-1)$$

10. ANOVA (1-way)

$$SS_{\text{Total}} = \Sigma X^2 - \frac{(\Sigma X)^2}{n_T}$$

$$SS_{\text{Treatments}} = \frac{(\Sigma X_A)^2}{n_A} + \frac{(\Sigma X_B)^2}{n_B} + \dots + \frac{(\Sigma X)^2}{n_T}$$

$$SS_{\text{Error}} = SS_{\text{Total}} - SS_{\text{Treatments}}$$

$$\text{d.f. (Total)} = (n_T - 1)$$

$$\text{d.f. (Treatment)} = (k - 1)$$

$$\text{d.f. (Error)} = (n_1 + n_2 + \dots + n_k - k)$$

$$HSD = \frac{q\sqrt{MS_{\text{error}}}}{\sqrt{n}}$$

$$n_{nm} = \frac{2 n_1 n_2}{n_1 + n_2}$$



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11. Ujian Kruskal-Wallis

$$H = \frac{12}{N(N+1)} \left( \frac{R_1^2}{n_1} + \frac{R_2^2}{n_2} + \dots + \frac{R_k^2}{n_k} \right) - 3(N+1)$$

$$N = n_1 + n_2 + \dots + n_k$$

$$\text{d.f.} = k - 1$$

Ujian perbandingan berganda:

$$\Delta \bar{R} = Z_{(\alpha/k (k-1))} \sqrt{\frac{N(N+1)}{12} \left( \frac{1}{n_i} + \frac{1}{n_j} \right)}$$

12. Ujian Friedman

$$Q = \frac{12}{n_k(k+1)} (R_1^2 + R_2^2 + \dots + R_k^2) - 3n(k+1)$$

$$\text{d.f.} = k - 1$$

Ujian perbandingan berganda:

$$\Delta R = Z_{(\alpha/k (k-1))} \sqrt{\frac{b k (K+1)}{6}}$$

13. Formula Sturges

$$k = 1 + 3.3 \log_{10} n$$

... 10/-

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14. Ujian Korelasi

$$R = \frac{n \Sigma xy - \Sigma x \Sigma y}{\sqrt{n \Sigma x^2 - (\Sigma x)^2} \sqrt{n \Sigma y^2 - (\Sigma y)^2}}$$

15. Analisis Regresi

$$y = mx + c$$

$$m = \frac{\Sigma xy - \frac{\Sigma x \Sigma y}{n}}{\Sigma x^2 - \frac{(\Sigma x)^2}{n}}$$

$$c = \frac{\Sigma y - m(\Sigma x)}{n}$$

$$SS_E = \Sigma y^2 - m \Sigma xy - \frac{(\Sigma y)^2}{n} + \frac{m \Sigma x \Sigma y}{n}$$

$$S_{yx} = \sqrt{\frac{SS_E}{n-2}}$$

$$16. \chi^2 = \frac{N(AD - BC)^2}{(A+B)(C+D)(A+C)(B+D)}$$

$$17. 99\% \text{ CI } \mu = \bar{X} \pm \left( t \times \frac{s}{\sqrt{n}} \right)$$

$$18. 99\% \text{ CI } \mu = \bar{X} \pm \left( z \times \frac{\sigma}{\sqrt{n}} \right)$$

$$19. Z = \frac{\bar{X} - \mu}{\sigma/\sqrt{n}}$$

-ooOoo-

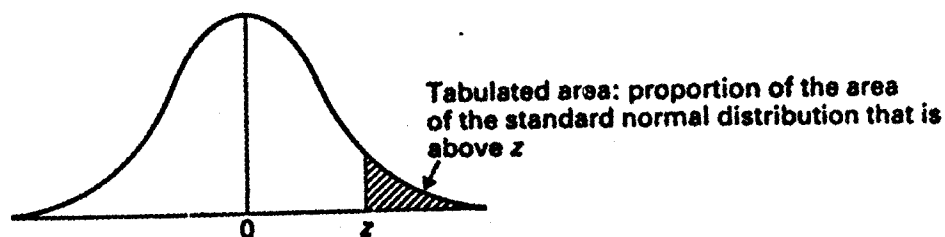
THE CORRELATION COEFFICIENT

Values of the correlation Coefficient for Different Levels of Significance (2 tail)

d.f.	.1	.05	.02	.01	.001
1.	.98769	.99692	.999507	.999877	.9999988
2.	.90000	.95000	.98000	.990000	.99900
3.	.8054	.8783	.93433	.95873	.99116
4.	.7293	.8114	.8822	.91720	.97406
5.	.6694	.7545	.8329	.8745	.95074
6.	.6215	.7067	.7887	.8343	.92493
7.	.5822	.6664	.7498	.7977	.8982
8.	.5494	.6319	.7155	.7646	.8721
9.	.5214	.6021	.6851	.7348	.8471
10.	.4973	.5760	.6581	.7079	.8233
11.	.4762	.5529	.6339	.6835	.8010
12.	.4575	.5324	.6120	.6614	.7800
13.	.4409	.5139	.5923	.6411	.7603
14.	.4259	.4973	.5742	.6226	.7420
15.	.4124	.4821	.5577	.6055	.7246

d.f. = degrees of freedom

Table A1 Areas in tail of the standard normal distribution.

Adapted from Table 3 of White *et al.* (1979) with permission of the authors and publishers.

z	Second decimal place of z									
	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641
0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
2.0	0.02275	0.02222	0.02169	0.02118	0.02068	0.02018	0.01970	0.01923	0.01876	0.01831
2.1	0.01786	0.01743	0.01700	0.01659	0.01618	0.01578	0.01539	0.01500	0.01463	0.01426
2.2	0.01390	0.01355	0.01321	0.01287	0.01255	0.01222	0.01191	0.01160	0.01130	0.01101
2.3	0.01072	0.01044	0.01017	0.00990	0.00964	0.00939	0.00914	0.00889	0.00866	0.00842
2.4	0.00820	0.00798	0.00776	0.00755	0.00734	0.00714	0.00695	0.00676	0.00657	0.00639
2.5	0.00621	0.00604	0.00587	0.00570	0.00554	0.00539	0.00523	0.00508	0.00494	0.00480
2.6	0.00466	0.00453	0.00440	0.00427	0.00415	0.00402	0.00391	0.00379	0.00368	0.00357
2.7	0.00347	0.00336	0.00326	0.00317	0.00307	0.00298	0.00289	0.00280	0.00272	0.00264
2.8	0.00256	0.00248	0.00240	0.00233	0.00226	0.00219	0.00212	0.00205	0.00199	0.00193
2.9	0.00187	0.00181	0.00175	0.00169	0.00164	0.00159	0.00154	0.00149	0.00144	0.00139
3.0	0.00135	0.00131	0.00126	0.00122	0.00118	0.00114	0.00111	0.00107	0.00104	0.00100
3.1	0.00097	0.00094	0.00090	0.00087	0.00084	0.00082	0.00079	0.00076	0.00074	0.00071
3.2	0.00069	0.00066	0.00064	0.00062	0.00060	0.00058	0.00056	0.00054	0.00052	0.00050
3.3	0.00048	0.00047	0.00045	0.00043	0.00042	0.00040	0.00039	0.00038	0.00036	0.00035
3.4	0.00034	0.00032	0.00031	0.00030	0.00029	0.00028	0.00027	0.00026	0.00025	0.00024
3.5	0.00023	0.00022	0.00022	0.00021	0.00020	0.00019	0.00019	0.00018	0.00017	0.00017
3.6	0.00016	0.00015	0.00015	0.00014	0.00014	0.00013	0.00013	0.00012	0.00012	0.00011
3.7	0.00011	0.00010	0.00010	0.00010	0.00009	0.00009	0.00008	0.00008	0.00008	0.00008
3.8	0.00007	0.00007	0.00007	0.00006	0.00006	0.00006	0.00006	0.00005	0.00005	0.00005
3.9	0.00005	0.00005	0.00004	0.00004	0.00004	0.00004	0.00004	0.00004	0.00003	0.00003

## Statistical Tables

Table A3 Percentage points of the *t* distribution.Adapted from Table 7 of White *et al.* (1979) with permission of authors and publishers.

d.f.	One-sided <i>P</i> value								
	0.25	0.1	0.05	0.025	0.01	0.005	0.0025	0.001	0.0005
	Two-sided <i>P</i> value								
	0.5	0.2	0.1	0.05	0.02	0.01	0.005	0.002	0.001
1	1.00	3.08	6.31	12.71	31.82	63.66	127.32	318.31	636.62
2	0.82	1.89	2.92	4.30	6.96	9.92	14.09	22.33	31.60
3	0.76	1.64	2.35	3.18	4.54	5.84	7.45	10.21	12.92
4	0.74	1.53	2.13	2.78	3.75	4.60	5.60	7.17	8.61
5	0.73	1.48	2.02	2.57	3.36	4.03	4.77	5.89	6.87
6	0.72	1.44	1.94	2.45	3.14	3.71	4.32	5.21	5.96
7	0.71	1.42	1.90	2.36	3.00	3.50	4.03	4.78	5.41
8	0.71	1.40	1.86	2.31	2.90	3.36	3.83	4.50	5.04
9	0.70	1.38	1.83	2.26	2.82	3.25	3.69	4.30	4.78
10	0.70	1.37	1.81	2.23	2.76	3.17	3.58	4.14	4.59
11	0.70	1.36	1.80	2.20	2.72	3.11	3.50	4.02	4.44
12	0.70	1.36	1.78	2.18	2.68	3.06	3.43	3.93	4.32
13	0.69	1.35	1.77	2.16	2.65	3.01	3.37	3.85	4.22
14	0.69	1.34	1.76	2.14	2.62	2.98	3.33	3.79	4.14
15	0.69	1.34	1.75	2.13	2.60	2.95	3.29	3.73	4.07
16	0.69	1.34	1.75	2.12	2.58	2.92	3.25	3.69	4.02
17	0.69	1.33	1.74	2.11	2.57	2.90	3.22	3.65	3.96
18	0.69	1.33	1.73	2.10	2.55	2.88	3.20	3.61	3.92
19	0.69	1.33	1.73	2.09	2.54	2.86	3.17	3.58	3.88
20	0.69	1.32	1.72	2.09	2.53	2.84	3.15	3.55	3.85
21	0.69	1.32	1.72	2.08	2.52	2.83	3.14	3.53	3.82
22	0.69	1.32	1.72	2.07	2.51	2.82	3.12	3.50	3.79
23	0.68	1.32	1.71	2.07	2.50	2.81	3.10	3.48	3.77
24	0.68	1.32	1.71	2.06	2.49	2.80	3.09	3.47	3.74
25	0.68	1.32	1.71	2.06	2.48	2.79	3.08	3.45	3.72
26	0.68	1.32	1.71	2.06	2.48	2.78	3.07	3.44	3.71
27	0.68	1.31	1.70	2.05	2.47	2.77	3.06	3.42	3.69
28	0.68	1.31	1.70	2.05	2.47	2.76	3.05	3.41	3.67
29	0.68	1.31	1.70	2.04	2.46	2.76	3.04	3.40	3.66
30	0.68	1.31	1.70	2.04	2.46	2.75	3.03	3.38	3.65
40	0.68	1.30	1.68	2.02	2.42	2.70	2.97	3.31	3.55
60	0.68	1.30	1.67	2.00	2.39	2.66	2.92	3.23	3.46
120	0.68	1.29	1.66	1.98	2.36	2.62	2.86	3.16	3.37
∞	0.67	1.28	1.65	1.96	2.33	2.58	2.81	3.09	3.29

**Taburan Poisson**

$X$  menandakan suatu pembolehubah dengan suatu taburan Poisson yang mempunyai jangkaan  $\mu$ . Sifir ini memberikan nilai  $P(X = k) = (e^{-\mu} \mu^k / k!)$  bagi berbagai nilai  $k$  dan  $\mu$ .

*Contoh.* Untuk  $\mu = 1.0$ ,

$$P(X = 1) = .368$$

$$P(X = 3) = .061$$

$$P(X \leq 2) = P(X = 0) + P(X = 1) + P(X = 2) \\ = .368 + .368 + .184 \\ = .920$$

$k$	$\mu = .1$	$\mu = .5$	$\mu = 1.0$	$\mu = 2.0$
0	.905	.607	.368	.135
1	.090	.303	.368	.271
2	.005	.076	.184	.271
3		.013	.061	.180
4		.002	.015	.090
5			.003	.036
6			.001	.012
7				.003
8				.001

$k$	$\mu = 3.0$	$\mu = 4.0$	$\mu = 5.0$	$\mu = 6.0$
0	.050	.018	.007	.002
1	.149	.073	.034	.015
2	.224	.147	.084	.045
3	.224	.195	.140	.089
4	.168	.195	.175	.134
5	.101	.156	.175	.161
6	.050	.104	.146	.138
7	.022	.060	.104	.103
8	.008	.030	.065	.069
9	.003	.013	.036	.041
10	.001	.005	.018	.023
11		.002	.008	.011
12		.001	.003	.005
13			.001	.002
14				.001
15				

$k$	$\mu = 7.0$	$\mu = 8.0$	$\mu = 9.0$	$\mu = 10.0$
0	.001	.003	.001	.002
1	.006	.011	.005	.008
2	.022	.029	.015	.019
3	.052	.057	.034	.038
4	.091	.092	.061	.063
5	.128	.122	.091	.090
6	.149	.140	.117	.113
7	.149	.140	.132	.125
8	.130	.124	.132	.125
9	.101	.099	.119	.114
10	.071	.072	.097	.095
11	.045	.048	.073	.073
12	.026	.030	.050	.052
13	.014	.017	.032	.035
14	.007	.009	.019	.022
15	.003	.005	.011	.013
16	.001	.002	.006	.007
17	.001		.003	.004
18			.001	.002
19				
20				
21				

TABLE III Critical values of  $t$ 

For any given  $df$ , the table shows the values of  $t$  corresponding to various levels of probability. Obtained  $t$  is significant at a given level if it is equal to or greater than the value shown in the table.

df	Level of significance for one-tailed test					
	.10	.05	.025	.01	.005	.0005
	Level of significance for two-tailed test					
	.20	.10	.05	.02	.01	.001
1	3.078	6.314	12.706	31.821	63.657	636.619
2	1.886	2.920	4.303	6.965	9.925	31.598
3	1.638	2.353	3.182	4.541	5.841	12.941
4	1.533	2.132	2.776	3.747	4.604	8.610
5	1.476	2.015	2.571	3.365	4.032	6.859
6	1.440	1.943	2.447	3.143	3.707	5.959
7	1.415	1.895	2.365	2.998	3.499	5.405
8	1.397	1.860	2.306	2.896	3.355	5.041
9	1.383	1.833	2.262	2.821	3.250	4.781
10	1.372	1.812	2.228	2.764	3.169	4.587
11	1.363	1.796	2.201	2.718	3.106	4.437
12	1.356	1.782	2.179	2.681	3.055	4.318
13	1.350	1.771	2.160	2.650	3.012	4.221
14	1.345	1.761	2.145	2.624	2.977	4.140
15	1.341	1.753	2.131	2.602	2.947	4.073
16	1.337	1.746	2.120	2.583	2.921	4.015
17	1.333	1.740	2.110	2.567	2.898	3.965
18	1.330	1.734	2.101	2.552	2.878	3.922
19	1.328	1.729	2.093	2.539	2.861	3.883
20	1.325	1.725	2.086	2.528	2.845	3.850
21	1.323	1.721	2.080	2.518	2.831	3.819
22	1.321	1.717	2.074	2.508	2.819	3.792
23	1.319	1.714	2.069	2.500	2.807	3.767
24	1.318	1.711	2.064	2.492	2.797	3.745
25	1.316	1.708	2.060	2.485	2.787	3.725
26	1.315	1.706	2.056	2.479	2.779	3.707
27	1.314	1.703	2.052	2.473	2.771	3.690
28	1.313	1.701	2.048	2.467	2.763	3.674
29	1.311	1.699	2.045	2.462	2.756	3.659
30	1.310	1.697	2.042	2.457	2.750	3.646
40	1.303	1.684	2.021	2.423	2.704	3.551
60	1.296	1.671	2.000	2.390	2.660	3.460
120	1.289	1.658	1.980	2.358	2.617	3.373
$\infty$	1.282	1.645	1.960	2.326	2.576	3.291

From R. A. Fisher and F. Yates, *Statistical Tables for Biological, Agricultural and Medical Research*, published by Longman Group Ltd., London (previously published by Oliver and Boyd Ltd., Edinburgh) and by permission of the authors and publishers.

TABLE IV Normal curve areas

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
3.1	.49903									
3.2	.49931									
3.3	.49952									
3.4	.49966									
3.5	.49977									
3.6	.49984									
3.7	.49989									
3.8	.49993									
3.9	.49995									
4.0	.50000									



TABLE V Chi square

Column headings indicate probability of chance  
deviation between O and E.

D.F. \ P	0.25	0.10	0.05	0.025	0.01	0.005
1.	1.323	2.706	3.841	5.024	6.635	7.879
2.	2.773	4.605	5.991	7.378	9.210	10.597
3.	4.108	6.251	7.815	9.348	11.345	12.838
4.	5.385	7.779	9.488	11.143	13.277	14.860
5.	6.626	9.236	11.071	12.833	15.086	16.750
6.	7.841	10.645	12.592	14.449	16.812	18.548
7.	9.037	12.017	14.067	16.013	18.475	20.278
8.	10.219	13.362	15.507	17.535	20.090	21.955
9.	11.389	14.684	16.919	19.023	21.666	23.589
10.	12.549	15.987	18.307	20.483	23.209	25.188
11.	13.701	17.275	19.675	21.920	24.725	26.757
12.	14.845	18.549	21.026	23.337	26.217	28.299
13.	15.984	19.812	22.362	24.736	27.688	29.819
14.	17.117	21.064	23.685	26.119	29.141	31.319
15.	18.245	22.307	24.996	27.488	30.578	32.801

Adapted from table of  $\chi^2$  appearing in *Handbook of Statistical Tables* by D. B. Owen, Addison-Wesley, 1962, p. 50. Reprinted by permission of the U.S. Atomic Energy Commission.

TABLE VII Critical Values of  $F$ 

[FMT 202]-8

The obtained  $F$  is significant at a given level if it is equal to or greater than the value shown in the table.  
0.05 (light row) and 0.01 (dark row) points for the distribution of  $F$

		Degrees of freedom for greater mean square																							
		1	2	3	4	5	6	7	8	9	10	11	12	14	16	20	24	30	40	50	75	100	200	500	$\infty$
Degrees of freedom for lesser mean square	1	161 4052	200 4999	216 5403	225 5625	230 5764	234 5859	237 5928	239 5981	241 6022	242 6056	243 6082	244 6106	245 6142	246 6169	248 6208	249 6234	250 6258	251 6286	252 6302	253 6323	253 6334	254 6352	254 6361	254 6366
	2	18.51 98.49	19.00 99.01	19.16 99.17	19.25 99.25	19.30 99.30	19.33 99.33	19.36 99.34	19.37 99.36	19.38 99.38	19.39 99.40	19.40 99.41	19.41 99.42	19.42 99.43	19.43 99.44	19.44 99.45	19.45 99.46	19.46 99.47	19.47 99.48	19.47 99.48	19.48 99.49	19.49 99.49	19.49 99.49	19.50 99.50	19.50 99.50
	3	10.13 34.12	9.55 30.81	9.28 29.46	9.12 28.71	9.01 28.24	8.94 27.91	8.88 27.67	8.84 27.49	8.81 27.34	8.78 27.23	8.76 27.13	8.74 27.05	8.71 26.92	8.69 26.83	8.66 26.69	8.64 26.60	8.62 26.50	8.60 26.41	8.58 26.30	8.57 26.27	8.56 26.23	8.54 26.18	8.54 26.14	8.53 26.12
	4	7.71 21.20	6.94 18.00	6.59 16.69	6.39 15.98	6.26 15.52	6.16 15.21	6.09 14.98	6.04 14.80	6.00 14.66	5.96 14.54	5.93 14.45	5.91 14.37	5.87 14.24	5.84 14.15	5.80 14.02	5.77 13.93	5.74 13.83	5.71 13.74	5.70 13.69	5.68 13.61	5.66 13.57	5.65 13.52	5.64 13.48	5.63 13.46
	5	6.61 16.26	5.79 13.27	5.41 12.06	5.19 11.39	5.05 10.97	4.95 10.67	4.88 10.45	4.82 10.27	4.78 10.15	4.74 10.05	4.70 9.96	4.68 9.89	4.64 9.77	4.60 9.68	4.56 9.55	4.53 9.47	4.50 9.38	4.46 9.29	4.44 9.24	4.42 9.17	4.40 9.13	4.38 9.07	4.37 9.04	4.36 9.02
	6	5.99 13.74	5.14 10.92	4.76 9.78	4.53 9.15	4.39 8.75	4.28 8.47	4.21 8.26	4.15 8.10	4.10 7.98	4.06 7.87	4.03 7.79	4.00 7.72	3.96 7.60	3.92 7.52	3.87 7.39	3.84 7.31	3.81 7.23	3.77 7.14	3.75 7.09	3.72 7.02	3.71 6.99	3.69 6.94	3.68 6.90	3.67 6.88
	7	5.59 12.25	4.74 9.55	4.35 8.45	4.12 7.85	3.97 7.46	3.87 7.19	3.79 7.00	3.73 6.84	3.68 6.71	3.63 6.62	3.60 6.54	3.57 6.47	3.52 6.35	3.49 6.27	3.44 6.15	3.41 6.07	3.38 5.98	3.34 5.90	3.32 5.85	3.29 5.78	3.28 5.75	3.25 5.70	3.24 5.67	3.23 5.65
	8	5.32 11.26	4.46 8.65	4.07 7.59	3.84 7.01	3.69 6.63	3.58 6.37	3.50 6.19	3.44 6.03	3.39 5.91	3.34 5.82	3.31 5.74	3.28 5.67	3.23 5.56	3.20 5.48	3.15 5.36	3.12 5.28	3.08 5.20	3.05 5.11	3.03 5.06	3.00 5.00	2.98 4.96	2.96 4.91	2.94 4.88	2.93 4.86
	9	5.12 10.56	4.26 8.02	3.86 6.99	3.63 6.42	3.48 6.06	3.37 5.80	3.29 5.62	3.23 5.47	3.18 5.35	3.13 5.26	3.10 5.18	3.07 5.11	3.02 5.00	2.98 4.92	2.93 4.80	2.90 4.73	2.86 4.64	2.82 4.56	2.80 4.51	2.77 4.45	2.76 4.41	2.73 4.36	2.72 4.33	2.71 4.31
	10	4.96 10.04	4.10 7.56	3.71 6.55	3.48 5.99	3.33 5.64	3.22 5.39	3.14 5.21	3.07 5.06	3.02 4.95	2.97 4.85	2.94 4.78	2.91 4.71	2.86 4.60	2.82 4.52	2.77 4.41	2.74 4.33	2.70 4.25	2.67 4.17	2.64 4.12	2.61 4.05	2.59 4.01	2.56 3.96	2.55 3.93	2.54 3.91
	11	4.84 9.65	3.98 7.20	3.59 6.22	3.36 5.67	3.20 5.32	3.09 5.07	3.01 4.88	2.95 4.74	2.90 4.63	2.86 4.54	2.82 4.46	2.79 4.40	2.74 4.29	2.70 4.21	2.65 4.10	2.61 4.02	2.57 3.94	2.53 3.86	2.50 3.80	2.47 3.74	2.45 3.70	2.42 3.66	2.41 3.62	2.40 3.60
	12	4.75 9.33	3.88 6.93	3.49 5.95	3.26 5.41	3.11 5.06	3.00 4.82	2.92 4.65	2.85 4.50	2.80 4.39	2.76 4.30	2.72 4.22	2.69 4.16	2.64 4.05	2.60 3.98	2.54 3.86	2.50 3.78	2.46 3.70	2.42 3.61	2.40 3.56	2.36 3.49	2.35 3.46	2.32 3.41	2.31 3.38	2.30 3.36
	13	4.67 9.07	3.80 6.70	3.41 5.74	3.18 5.20	3.02 4.86	2.92 4.62	2.84 4.44	2.77 4.30	2.72 4.19	2.67 4.10	2.63 4.02	2.60 3.96	2.55 3.85	2.51 3.78	2.46 3.67	2.42 3.59	2.38 3.51	2.34 3.42	2.32 3.37	2.28 3.30	2.26 3.27	2.24 3.21	2.22 3.18	2.21 3.16
	14	4.60 8.86	3.74 6.51	3.34 5.56	3.11 5.03	2.96 4.69	2.85 4.46	2.77 4.28	2.70 4.14	2.65 4.03	2.60 3.94	2.56 3.86	2.63 3.80	2.48 3.70	2.44 3.62	2.39 3.51	2.35 3.43	2.31 3.34	2.27 3.26	2.24 3.21	2.21 3.14	2.19 3.11	2.16 3.06	2.14 3.02	2.13 3.00
	15	4.54 8.68	3.68 6.36	3.29 5.42	3.06 4.89	2.90 4.56	2.79 4.32	2.70 4.14	2.64 4.00	2.59 3.89	2.55 3.80	2.51 3.73	2.48 3.67	2.43 3.56	2.39 3.48	2.33 3.36	2.29 3.29	2.25 3.20	2.21 3.12	2.18 3.07	2.15 3.00	2.12 2.97	2.10 2.92	2.08 2.89	2.07 2.87

TABLE VII (continued)

0.05 (light row) and 0.01 (dark row) points for the distribution of  $F$

		Degrees of freedom for greater mean square																							
		1	2	3	4	5	6	7	8	9	10	11	12	14	16	20	24	30	40	50	75	100	200	500	$\infty$
Degrees of freedom for lesser mean square	16	4.49 8.53	3.63 6.23	3.24 5.29	3.01 4.77	2.85 4.44	2.74 4.20	2.66 4.03	2.59 3.89	2.54 3.78	2.49 3.69	2.45 3.61	2.42 3.55	2.37 3.45	2.33 3.37	2.28 3.25	2.24 3.18	2.20 3.10	2.16 3.01	2.13 2.96	2.09 2.89	2.07 2.86	2.04 2.80	2.02 2.77	2.01 2.75
	17	4.45 8.40	3.59 6.11	3.20 5.18	2.96 4.67	2.81 4.34	2.70 4.10	2.62 3.93	2.55 3.79	2.50 3.68	2.45 3.59	2.41 3.52	2.38 3.45	2.33 3.35	2.29 3.27	2.23 3.16	2.19 3.08	2.15 3.00	2.11 2.92	2.08 2.86	2.04 2.79	2.02 2.76	1.99 2.70	1.97 2.67	1.96 2.65
	18	4.41 8.28	3.55 6.01	3.16 5.09	2.93 4.58	2.77 4.25	2.66 4.01	2.58 3.85	2.51 3.71	2.46 3.60	2.41 3.51	2.37 3.44	2.34 3.37	2.29 3.27	2.25 3.19	2.19 3.07	2.15 3.00	2.11 2.91	2.07 2.83	2.04 2.78	2.00 2.71	1.98 2.68	1.95 2.62	1.93 2.59	1.92 2.57
	19	4.38 8.18	3.52 5.93	3.13 5.01	2.90 4.50	2.74 4.17	2.63 3.94	2.55 3.77	2.48 3.63	2.43 3.52	2.38 3.43	2.34 3.36	2.31 3.30	2.26 3.19	2.21 3.12	2.15 3.00	2.11 2.92	2.07 2.84	2.02 2.76	2.00 2.70	1.96 2.63	1.94 2.60	1.91 2.54	1.90 2.51	1.88 2.49
	20	4.35 8.10	3.49 5.85	3.10 4.94	2.87 4.43	2.71 4.10	2.60 3.87	2.52 3.71	2.45 3.56	2.40 3.45	2.35 3.37	2.31 3.30	2.28 3.23	2.23 3.13	2.18 3.05	2.12 2.94	2.08 2.86	2.04 2.77	1.99 2.69	1.96 2.63	1.92 2.56	1.90 2.53	1.87 2.47	1.85 2.44	1.84 2.42
	21	4.32 8.02	3.47 5.78	3.07 4.87	2.84 4.37	2.68 4.04	2.57 3.81	2.49 3.65	2.42 3.51	2.37 3.40	2.32 3.31	2.28 3.24	2.25 3.17	2.20 3.07	2.15 2.99	2.09 2.88	2.05 2.80	2.00 2.72	1.96 2.63	1.93 2.58	1.89 2.51	1.87 2.47	1.84 2.42	1.82 2.38	1.81 2.36
	22	4.30 7.94	3.44 5.72	3.05 4.82	2.82 4.31	2.66 3.99	2.55 3.76	2.47 3.59	2.40 3.45	2.35 3.35	2.30 3.26	2.26 3.18	2.23 3.12	2.18 3.02	2.13 2.94	2.07 2.83	2.03 2.75	1.98 2.67	1.93 2.58	1.91 2.53	1.87 2.46	1.84 2.42	1.81 2.37	1.80 2.33	1.78 2.31
	23	4.28 7.88	3.42 5.66	3.03 4.76	2.80 4.26	2.64 3.94	2.53 3.71	2.45 3.54	2.38 3.41	2.32 3.30	2.28 3.21	2.24 3.14	2.20 3.07	2.14 2.97	2.10 2.89	2.04 2.78	2.00 2.70	1.96 2.62	1.91 2.53	1.88 2.48	1.84 2.41	1.82 2.37	1.79 2.32	1.77 2.28	1.76 2.26
	24	4.26 7.82	3.40 5.61	3.01 4.72	2.78 4.22	2.62 3.90	2.51 3.67	2.43 3.50	2.36 3.36	2.30 3.25	2.26 3.17	2.22 3.09	2.18 3.03	2.13 2.93	2.09 2.85	2.02 2.74	1.98 2.66	1.94 2.58	1.89 2.49	1.86 2.44	1.82 2.36	1.80 2.33	1.76 2.27	1.74 2.23	1.73 2.21
	25	4.24 7.77	3.38 5.57	2.99 4.68	2.76 4.18	2.60 3.86	2.49 3.63	2.41 3.46	2.34 3.32	2.28 3.21	2.24 3.13	2.20 3.05	2.16 2.99	2.11 2.89	2.06 2.81	2.00 2.70	1.96 2.62	1.92 2.54	1.87 2.45	1.84 2.40	1.80 2.32	1.77 2.29	1.74 2.23	1.72 2.19	1.71 2.17
	26	4.22 7.72	3.37 5.53	2.89 4.64	2.74 4.14	2.59 3.82	2.47 3.59	2.39 3.42	2.32 3.29	2.27 3.17	2.22 3.09	2.18 3.02	2.15 2.96	2.10 2.86	2.05 2.77	1.99 2.66	1.95 2.58	1.90 2.50	1.85 2.41	1.82 2.36	1.78 2.28	1.76 2.25	1.72 2.19	1.70 2.15	1.69 2.13
	27	4.21 7.68	3.35 5.49	2.96 4.60	2.73 4.11	2.57 3.79	2.46 3.56	2.37 3.39	2.30 3.26	2.25 3.14	2.20 3.06	2.16 2.98	2.13 2.93	2.08 2.83	2.03 2.74	1.97 2.63	1.93 2.55	1.88 2.47	1.84 2.38	1.80 2.33	1.76 2.25	1.74 2.21	1.71 2.16	1.68 2.12	1.67 2.10
	28	4.20 7.64	3.34 5.45	2.95 4.57	2.71 4.07	2.56 3.76	2.44 3.53	2.36 3.36	2.29 3.23	2.24 3.11	2.19 3.03	2.15 2.95	2.12 2.90	2.06 2.80	2.02 2.71	1.96 2.60	1.91 2.52	1.87 2.44	1.81 2.35	1.78 2.30	1.75 2.22	1.72 2.18	1.69 2.13	1.67 2.09	1.65 2.06
	29	4.18 7.60	3.33 5.52	2.93 4.54	2.70 4.04	2.54 3.73	2.43 3.50	2.35 3.32	2.28 3.20	2.22 3.08	2.18 3.00	2.14 2.92	2.10 2.87	2.05 2.77	2.00 2.68	1.94 2.57	1.90 2.49	1.85 2.41	1.80 2.32	1.77 2.27	1.73 2.19	1.71 2.15	1.68 2.10	1.65 2.06	1.64 2.03
	30	4.17 7.56	3.32 5.39	2.92 4.51	2.69 4.02	2.53 3.70	2.42 3.47	2.34 3.30	2.27 3.17	2.21 3.06	2.16 2.98	2.12 2.90	2.09 2.84	2.04 2.74	1.99 2.66	1.93 2.55	1.89 2.47	1.84 2.38	1.79 2.29	1.76 2.24	1.72 2.16	1.69 2.13	1.66 2.07	1.64 2.03	1.62 2.01

TABLE VII (continued)

[FMT 202]-9

0.05 (light row) and 0.01 (dark row) points for the distribution of F

		Degrees of freedom for greater mean square																							
		1	2	3	4	5	6	7	8	9	10	11	12	14	16	20	24	30	40	50	75	100	200	500	$\infty$
Degrees of freedom for lesser mean square	32	4.15 7.50	3.30 5.34	2.90 4.46	2.67 3.97	2.51 3.66	2.40 3.42	2.32 3.25	2.25 3.12	2.19 3.01	2.14 2.94	2.10 2.86	2.07 2.80	2.02 2.70	1.97 2.62	1.91 2.51	1.86 2.42	1.82 2.34	1.76 2.25	1.74 2.20	1.69 2.12	1.67 2.06	1.64 2.02	1.61 1.98	1.59 1.96
	34	4.13 7.44	3.28 5.29	2.88 4.42	2.65 3.93	2.49 3.61	2.38 3.38	2.30 3.21	2.23 3.08	2.17 2.97	2.12 2.89	2.08 2.82	2.05 2.76	2.00 2.66	1.95 2.58	1.89 2.47	1.84 2.38	1.80 2.30	1.74 2.21	1.71 2.15	1.67 2.08	1.64 2.04	1.61 1.98	1.59 1.94	1.57 1.91
	36	4.11 7.39	3.26 5.25	2.86 4.38	2.63 3.89	2.48 3.58	2.36 3.35	2.28 3.18	2.21 3.04	2.15 2.94	2.10 2.86	2.06 2.78	2.03 2.72	1.99 2.62	1.93 2.54	1.87 2.43	1.82 2.35	1.78 2.26	1.72 2.17	1.69 2.12	1.65 2.04	1.62 2.00	1.59 1.94	1.56 1.90	1.55 1.87
	38	4.10 7.35	3.25 5.21	2.85 4.34	2.62 3.86	2.46 3.54	2.35 3.32	2.26 3.15	2.19 3.02	2.14 2.91	2.09 2.82	2.05 2.75	2.02 2.69	1.96 2.59	1.92 2.51	1.85 2.40	1.80 2.32	1.76 2.22	1.71 2.14	1.67 2.08	1.63 2.00	1.60 1.97	1.57 1.90	1.54 1.86	1.53 1.84
	40	4.08 7.31	3.23 5.18	2.84 4.31	2.61 3.83	2.45 3.51	2.34 3.29	2.25 3.12	2.18 2.99	2.12 2.88	2.07 2.80	2.04 2.73	2.00 2.66	1.95 2.56	1.90 2.49	1.84 2.37	1.79 2.29	1.74 2.20	1.69 2.11	1.66 2.05	1.61 1.97	1.59 1.94	1.55 1.88	1.53 1.84	1.51 1.81
	42	4.07 7.27	3.22 5.15	2.83 4.29	2.59 3.80	2.44 3.49	2.32 3.26	2.24 3.10	2.17 2.96	2.11 2.86	2.06 2.77	2.02 2.70	1.90 2.64	1.94 2.54	1.89 2.46	1.82 2.35	1.78 2.26	1.73 2.17	1.68 2.08	1.64 2.02	1.60 1.94	1.57 1.91	1.54 1.85	1.51 1.80	1.49 1.78
	44	4.06 7.24	3.21 5.12	2.82 4.26	2.58 3.78	2.43 3.46	2.31 3.24	2.23 3.07	2.16 2.94	2.10 2.84	2.05 2.75	2.01 2.68	1.98 2.62	1.92 2.52	1.88 2.44	1.81 2.32	1.76 2.24	1.72 2.15	1.66 2.06	1.63 2.09	1.58 1.92	1.56 1.88	1.52 1.82	1.50 1.78	1.48 1.75
	46	4.05 7.21	3.20 5.10	2.81 4.24	2.57 3.76	2.42 3.44	2.30 3.22	2.22 3.05	2.14 2.92	2.09 2.82	2.04 2.73	2.00 2.66	1.97 2.60	1.91 2.50	1.87 2.42	1.80 2.30	1.75 2.22	1.71 2.13	1.65 2.04	1.62 1.98	1.57 1.90	1.54 1.86	1.51 1.80	1.48 1.76	1.46 1.72
	48	4.04 7.19	3.19 5.08	2.80 4.22	2.56 3.74	2.41 3.42	2.30 3.20	2.21 3.04	2.14 2.90	2.08 2.80	2.03 2.71	1.99 2.64	1.96 2.58	1.90 2.48	1.86 2.40	1.79 2.28	1.74 2.20	1.70 2.11	1.64 2.02	1.61 1.96	1.56 1.88	1.53 1.84	1.50 1.78	1.47 1.73	1.45 1.70
	50	4.03 7.17	3.18 5.06	2.79 4.20	2.56 3.72	2.40 3.41	2.29 3.18	2.20 3.02	2.13 2.88	2.07 2.78	2.02 2.70	1.98 2.62	1.95 2.56	1.90 2.46	1.85 2.39	1.78 2.26	1.74 2.18	1.69 2.10	1.63 2.00	1.60 1.94	1.55 1.86	1.52 1.82	1.48 1.76	1.46 1.71	1.44 1.68
	55	4.02 7.12	3.17 5.01	2.78 4.16	2.54 3.68	2.38 3.37	2.27 3.15	2.18 2.98	2.11 2.85	2.05 2.75	2.00 2.66	1.97 2.59	1.93 2.53	1.88 2.43	1.83 2.35	1.76 2.23	1.72 2.15	1.67 2.06	1.61 1.96	1.58 1.90	1.52 1.82	1.50 1.78	1.46 1.71	1.43 1.66	1.41 1.64
	60	4.00 7.08	3.15 4.98	2.76 4.13	2.52 3.65	2.37 3.34	2.25 3.12	2.17 2.95	2.10 2.82	2.04 2.72	1.99 2.63	1.95 2.56	1.92 2.50	1.86 2.40	1.81 2.32	1.75 2.20	1.70 2.12	1.65 2.03	1.59 1.93	1.56 1.87	1.50 1.79	1.48 1.74	1.44 1.68	1.41 1.63	1.39 1.60
	65	3.99 7.04	3.14 4.95	2.75 4.10	2.51 3.62	2.36 3.31	2.24 3.09	2.15 2.93	2.08 2.79	2.02 2.70	1.98 2.61	1.94 2.54	1.90 2.47	1.85 2.37	1.80 2.30	1.73 2.18	1.68 2.09	1.63 2.00	1.57 1.90	1.54 1.84	1.49 1.76	1.46 1.71	1.42 1.64	1.39 1.60	1.37 1.56
	70	3.98 7.01	3.13 4.92	2.74 4.08	2.50 3.60	2.35 3.29	2.23 3.07	2.14 2.91	2.07 2.77	2.01 2.67	1.97 2.59	1.93 2.51	1.89 2.45	1.84 2.35	1.79 2.28	1.72 2.15	1.67 2.07	1.62 1.98	1.56 1.88	1.53 1.82	1.47 1.74	1.45 1.69	1.40 1.62	1.37 1.56	1.35 1.53
	80	3.96 6.96	3.11 4.88	2.72 4.04	2.48 3.56	2.33 3.25	2.21 3.04	2.12 2.87	2.05 2.74	1.99 2.64	1.95 2.55	1.91 2.48	1.88 2.41	1.82 2.32	1.77 2.24	1.70 2.11	1.65 2.03	1.60 1.94	1.54 1.84	1.51 1.78	1.45 1.70	1.42 1.65	1.38 1.57	1.35 1.52	1.32 1.49

0.05 (light row) and 0.01 (dark row) points for the distribution of F

		Degrees of freedom for greater mean square																							
		1	2	3	4	5	6	7	8	9	10	11	12	14	16	20	24	30	40	50	75	100	200	500	$\infty$
100	Degrees of freedom for lesser mean square	3.94	3.09	2.70	2.46	2.30	2.19	2.10	2.03	1.97	1.92	1.88	1.85	1.79	1.75	1.68	1.63	1.57	1.51	1.48	1.42	1.39	1.34	1.30	1.28
		6.90	4.82	3.98	3.51	3.20	2.99	2.82	2.69	2.59	2.51	2.43	2.36	2.26	2.19	2.06	1.98	1.89	1.79	1.73	1.64	1.59	1.51	1.46	1.43
125	Degrees of freedom for lesser mean square	3.92	3.07	2.68	2.44	2.29	2.17	2.08	2.01	1.95	1.90	1.86	1.83	1.77	1.72	1.65	1.60	1.55	1.49	1.45	1.39	1.36	1.31	1.27	1.25
		6.84	4.78	3.94	3.47	3.17	2.95	2.79	2.65	2.56	2.47	2.40	2.33	2.23	2.15	2.03	1.94	1.85	1.75	1.68	1.59	1.54	1.46	1.40	1.37
150	Degrees of freedom for lesser mean square	3.91	3.06	2.67	2.43	2.27	2.16	2.07	2.00	1.94	1.89	1.85	1.82	1.76	1.71	1.64	1.59	1.54	1.47	1.44	1.37	1.34	1.29	1.25	1.22
		6.81	4.75	3.91	3.44	3.13	2.92	2.76	2.62	2.53	2.44	2.37	2.30	2.20	2.12	2.00	1.91	1.83	1.72	1.66	1.56	1.51	1.43	1.37	1.33
200	Degrees of freedom for lesser mean square	3.89	3.04	2.65	2.41	2.26	2.14	2.05	1.98	1.92	1.87	1.83	1.80	1.74	1.69	1.62	1.57	1.52	1.45	1.42	1.35	1.32	1.26	1.22	1.19
		6.76	4.71	3.88	3.41	3.11	2.90	2.73	2.60	2.50	2.41	2.34	2.28	2.17	2.09	1.97	1.88	1.79	1.69	1.62	1.53	1.48	1.39	1.33	1.28
400	Degrees of freedom for lesser mean square	3.86	3.02	2.62	2.39	2.23	2.12	2.03	1.96	1.90	1.85	1.81	1.78	1.72	1.67	1.60	1.54	1.49	1.42	1.38	1.32	1.28	1.22	1.16	1.13
		6.70	4.66	3.83	3.36	3.06	2.85	2.69	2.55	2.46	2.37	2.29	2.23	2.12	2.04	1.92	1.84	1.74	1.64	1.57	1.47	1.42	1.32	1.24	1.19
1000	Degrees of freedom for lesser mean square	3.85	3.00	2.61	2.38	2.22	2.10	2.02	1.95	1.89	1.84	1.80	1.76	1.70	1.65	1.58	1.53	1.47	1.41	1.36	1.30	1.26	1.19	1.13	1.08
		6.66	4.62	3.80	3.34	3.04	2.82	2.66	2.53	2.43	2.34	2.26	2.20	2.09	2.01	1.89	1.81	1.71	1.61	1.54	1.44	1.38	1.28	1.19	1.11
$\infty$	Degrees of freedom for lesser mean square	3.84	2.99	2.60	2.37	2.21	2.09	2.01	1.94	1.88	1.83	1.79	1.75	1.69	1.64	1.57	1.52	1.46	1.40	1.35	1.28	1.24	1.17	1.11	1.00
		6.64	4.60	3.78	3.32	3.02	2.80	2.64	2.51	2.41	2.32	2.24	2.18	2.07	1.99	1.87	1.79	1.69	1.59	1.52	1.41	1.36	1.25	1.15	1.00

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Wilcoxon table

This table gives the significance probabilities for the Wilcoxon signed-rank test for paired comparisons, for various selected values of the test statistic  $W$  = sum of all signed ranks. The significance probabilities included in the table are the ones closest to the commonly used levels of significance  $\alpha = .10$ ,  $\alpha = .05$ , and  $\alpha = .01$ . Thus the table may be used to obtain the appropriate critical value of  $W$  for a given value of  $\alpha$ , the level of significance.

The critical values  $c$  in the table correspond to the critical value for a one-sided test which rejects for large values of  $W$ . If the test is one-sided, and rejects for small (negative) values of  $W$ , then the critical value is  $-c$ , where  $c$  is the value in the table for which  $P(W \geq c)$  = desired level of significance. If the test is two-sided, then the critical value  $c$  is determined by finding the value in the table for which  $P(W \geq c) = 1/2 \alpha$ , where  $\alpha$  is the desired level of significance. In this case the test is to reject  $H_0$  if  $W \leq -c$  or  $W \geq c$ .

Examples

- (a) The test is one-sided and rejects for large values of  $W$ . Suppose  $\alpha = .05$  and  $n = 8$ . Then the critical value is  $c = 24$ , since  $P(W \geq c) = .055$ , and .055 is closest to the desired level  $\alpha = .05$ . Thus, the test rejects  $H_0$  if  $W \geq 24$ , and accepts otherwise.
- (b) The test is one-sided and rejects for small (negative) values of  $W$ . Suppose  $\alpha = .10$  and  $n = 12$ . The critical value is  $-34$ , since  $P(W \geq 34) = .102$ , and .102 is the value closest to .10. Thus the test rejects  $H_0$  if  $W \leq -34$ .
- (c) The test is two-sided. Suppose  $\alpha = .05$  and  $n = 20$ . Then the critical values are 106 and  $-106$ , since  $P(W \geq 106) = .024$ , and .024 is the value closest to .025 ( $= 1/2 \alpha$ ). Thus the test rejects  $H_0$  if  $W \leq -106$  or  $W \geq 106$ .

n		c		P(W ≥ c)		n		c		P(W ≥ c)		n		c		P(W ≥ c)	
1	1	.500	8	32	.012	12	58	.010	16	88	.011	20	124	.010	24	.010	
2	3	.250	9	28	.027	13	50	.026	17	76	.025	21	106	.024	25	.024	
3	6	.125	10	24	.055	14	44	.046	18	64	.046	22	98	.045	26	.045	
4	10	.062	11	20	.098	15	34	.102	19	52	.102	23	88	.101	27	.101	
5	15	.031	12	16	.125	16	28	.125	20	44	.125	24	76	.125	28	.125	
6	21	.016	13	13	.159	17	24	.159	21	40	.159	25	72	.159	29	.159	
7	28	.008	14	11	.199	18	20	.199	22	36	.199	26	68	.199	30	.199	
8	36	.003	15	9	.249	19	16	.249	23	32	.249	27	64	.249	33	.249	
9	45	.001	16	8	.309	20	14	.309	24	28	.309	28	60	.309	36	.309	
10	55	.000	17	7	.379	21	12	.379	25	24	.379	29	56	.379	39	.379	
11	66	.000	18	6	.459	22	11	.459	26	22	.459	30	52	.459	40	.459	
12	78	.000	19	5	.549	23	10	.549	27	20	.549	31	48	.549	42	.549	
13	91	.000	20	4	.649	24	9	.649	28	18	.649	32	44	.649	44	.649	
14	105	.000	21	3	.759	25	8	.759	29	16	.759	33	40	.759	46	.759	
15	120	.000	22	2	.879	26	7	.879	30	14	.879	34	36	.879	48	.879	
16	136	.000	23	1	.979	27	6	.979	31	12	.979	35	32	.979	50	.979	
17	153	.000	24	0	1.000	28	5	1.000	32	10	1.000	36	28	1.000	52	1.000	
18	171	.000	25	0	1.000	29	4	1.000	33	8	1.000	37	24	1.000	54	1.000	
19	190	.000	26	0	1.000	30	3	1.000	34	6	1.000	38	20	1.000	56	1.000	
20	210	.000	27	0	1.000	31	2	1.000	35	4	1.000	39	16	1.000	58	1.000	
21	231	.000	28	0	1.000	32	1	1.000	36	2	1.000	40	12	1.000	60	1.000	
22	253	.000	29	0	1.000	33	0	1.000	37	0	1.000	41	8	1.000	62	1.000	
23	276	.000	30	0	1.000	34	0	1.000	38	0	1.000	42	6	1.000	64	1.000	
24	300	.000	31	0	1.000	35	0	1.000	39	0	1.000	43	4	1.000	66	1.000	
25	325	.000	32	0	1.000	36	0	1.000	40	0	1.000	44	2	1.000	68	1.000	
26	351	.000	33	0	1.000	37	0	1.000	41	0	1.000	45	0	1.000	70	1.000	
27	378	.000	34	0	1.000	38	0	1.000	42	0	1.000	46	0	1.000	72	1.000	
28	406	.000	35	0	1.000	39	0	1.000	43	0	1.000	47	0	1.000	74	1.000	
29	435	.000	36	0	1.000	40	0	1.000	44	0	1.000	48	0	1.000	76	1.000	
30	465	.000	37	0	1.000	41	0	1.000	45	0	1.000	49	0	1.000	78	1.000	
31	496	.000	38	0	1.000	42	0	1.000	46	0	1.000	50	0	1.000	80	1.000	
32	528	.000	39	0	1.000	43	0	1.000	47	0	1.000	51	0	1.000	82	1.000	
33	561	.000	40	0	1.000	44	0	1.000	48	0	1.000	52	0	1.000	84	1.000	
34	595	.000	41	0	1.000	45	0	1.000	49	0	1.000	53	0	1.000	86	1.000	
35	630	.000	42	0	1.000	46	0	1.000	50	0	1.000	54	0	1.000	88	1.000	
36	666	.000	43	0	1.000	47	0	1.000	51	0	1.000	55	0	1.000	90	1.000	
37	703	.000	44	0	1.000	48	0	1.000	52	0	1.000	56	0	1.000	92	1.000	
38	741	.000	45	0	1.000	49	0	1.000	53	0	1.000	57	0	1.000	94	1.000	
39	780	.000	46	0	1.000	50	0	1.000	54	0	1.000	58	0	1.000	96	1.000	
40	820	.000	47	0	1.000	51	0	1.000	55	0	1.000	59	0	1.000	98	1.000	
41	861	.000	48	0	1.000	52	0	1.000	56	0	1.000	60	0	1.000	100	1.000	
42	903	.000	49	0	1.000	53	0	1.000	57	0	1.000	61	0	1.000			
43	946	.000	50	0	1.000	54	0	1.000	58	0	1.000	62	0	1.000			
44	990	.000	51	0	1.000	55	0	1.000	59	0	1.000	63	0	1.000			
45	1035	.000	52	0	1.000	56	0	1.000	60	0	1.000	64	0	1.000			
46	1081	.000	53	0	1.000	57	0	1.000	61	0	1.000	65	0	1.000			
47	1128	.000	54	0	1.000	58	0	1.000	62	0	1.000	66	0	1.000			
48	1176	.000	55	0	1.000	59	0	1.000	63	0	1.000	67	0	1.000			
49	1225	.000	56	0	1.000	60	0	1.000	64	0	1.000	68	0	1.000			
50	1275	.000	57	0	1.000	61	0	1.000	65	0	1.000	69	0	1.000			
51	1326	.000	58	0	1.000	62	0	1.000	66	0	1.000	70	0	1.000			
52	1378	.000	59	0	1.000	63	0	1.000	67	0	1.000	71	0	1.000			
53	1431	.000	60	0	1.000	64	0	1.000	68	0	1.000	72	0	1.000			
54	1485	.000	61	0	1.000	65	0	1.000	69	0	1.000	73	0	1.000			
55	1540	.000	62	0	1.000	66	0	1.000	70	0	1.000	74	0	1.000			
56	1596	.000	63	0	1.000	67	0	1.000	71	0	1.000	75	0	1.000			
57	1653	.000	64	0	1.000	68	0	1.000	72	0	1.000	76	0	1.000			
58	1711	.000	65	0	1.000	69	0	1.000	73	0	1.000	77	0	1.000			
59	1770	.000	66	0	1.000	70	0	1.000	74	0	1.000	78	0	1.000			
60	1830	.000	67	0	1.000	71	0	1.000	75	0	1.000	79	0	1.000			
61	1891	.000	68	0	1.000	72	0	1.000	76	0	1.000	80	0	1.000			
62	1953	.000	69	0	1.000	73	0	1.000	77	0	1.000	81	0	1.000			
63	2016	.000	70	0	1.000	74	0	1.000	78	0	1.000	82	0	1.000			
64	2081	.000	71	0	1.000	75	0	1.000	79	0	1.000	83	0	1.000			
65	2147	.000	72	0	1.000	76	0	1.000	80	0	1.000	84	0	1.000			
66	2214	.000	73	0	1.000	77	0	1.000	81	0	1.000	85	0	1.000			
67	2283	.000	74	0	1.000	78	0	1.000	82	0	1.000	86	0	1.000			
68	2353	.000	75	0	1.000	79	0	1.000	83	0	1.000	87	0	1.000			
69	2424	.000	76	0	1.000	80	0	1.000	84	0	1.000	88	0	1.000			
70	2496	.000	77	0	1.000	81	0	1.000	85	0	1.000	89	0	1.000			
71	2569	.000	78	0	1.000	82	0	1.000	86	0	1.000	90	0	1.000			
72	2643	.000	79	0	1.000	83	0	1.000	87	0	1.000	91	0	1.000			
73	2718	.000	80	0	1.000	84	0	1.000	88	0	1.000	92	0	1.000			
74	2794	.000	81	0	1.000	85	0	1.000	89	0	1.000	93	0	1.000			
75	2871	.000	82	0	1.000	86	0	1.000	90	0	1.000	94	0	1.000			
76	2950	.000	83	0	1.000	87	0	1.000	91	0	1.000	95	0	1.000			
77	3030	.000	84	0	1.000	88	0	1.000	92	0	1.000	96	0	1.000			
78	3111	.000	85	0	1.000	89	0	1.000	93	0	1.000	97	0	1.000			
79	3193	.000	86	0	1.000	90	0	1.000	94	0	1.000	98	0	1.000			
80	3276	.000	87	0	1.000	91	0	1.000	95	0	1.000	99	0	1.000			
81	3360	.000	88	0	1.000	92	0	1.000	96	0	1.000	100	0	1.000			
82	3445	.000	89	0	1.000	93	0	1.000	97	0	1.000						
83	3531	.000	90	0	1.000	94	0	1.000	98	0	1.000						
84	3618	.000	91	0	1.000	95	0	1.000	99	0	1.000						
85	3706	.000	92	0	1.000	96	0	1.000	100	0	1.000						
86	3795	.000	93	0	1.000	97	0	1.000									
87	3885	.000	94	0	1.000	98	0	1.000									
88	3976	.000	95	0	1.000	99	0	1.000									
89	4068	.000	96	0	1.000	100	0	1.000									
90	4161	.000	97	0	1.000												
91	4255	.000	98	0	1.000												
92	4350	.000	99	0	1.000												
93	4446	.000	100	0	1.000												
94	4543	.000															
95	4641	.000															
96	4740	.000															
97	4840	.000															
98	4941	.000															
99	5043	.000															

TABLE IX Critical values of  $U$ 

$n_1$	$n_2$	0.10	0.05	0.025	0.01	0.005	0.001
1	1						
2	2						
3	3						
4	4						
5	5						
6	6						
7	7						
8	8						
9	9						
10	10						
11	11						
12	12						
13	13						
14	14						
15	15						
16	16						
17	17						
18	18						
19	19						
20	20						
21	21						
22	22						
23	23						
24	24						
25	25						
26	26						
27	27						
28	28						
29	29						
30	30						
31	31						
32	32						
33	33						
34	34						
35	35						
36	36						
37	37						
38	38						
39	39						
40	40						
41	41						
42	42						
43	43						
44	44						
45	45						
46	46						
47	47						
48	48						
49	49						
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67	67						
68	68						
69	69						
70	70						
71	71						
72	72						
73	73						
74	74						
75	75						
76	76						
77	77						
78	78						
79	79						
80	80						
81	81						
82	82						
83	83						
84	84						
85	85						
86	86						
87	87						
88	88						
89	89						
90	90						
91	91						
92	92						
93	93						
94	94						
95	95						
96	96						
97	97						
98	98						
99	99						
100	100						

TABLE IX (continued)

$n_1$	$n_2$	0.10	0.05	0.025	0.01	0.005	0.001
101	101						
102	102						
103	103						
104	104						
105	105						
106	106						
107	107						
108	108						
109	109						
110	110						
111	111						
112	112						
113	113						
114	114						
115	115						
116	116						
117	117						
118	118						
119	119						
120	120						
121	121						
122	122						
123	123						
124	124						
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126	126						
127	127						
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129	129						
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132	132						
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136	136						
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138	138						
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142	142						
143	143						
144	144						
145	145						
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147	147						
148	148						
149	149						
150	150						
151	151						
152	152						
153	153						
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162	162						
163	163						
164	164						
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179	179						
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182	182						
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184	184						
185	185						
186	186						
187	187						
188	188						
189	189						
190	190						
191	191						
192	192						
193	193						
194	194						
195	195						
196	196						
197	197						
198	198						
199	199						
200	200						

TABLE IX (continued)

$n_1$	$n_2$	0.10	0.05	0.025	0.01	0.005	0.001
201	201						
202	202						
203	203						
204	204						
205	205						
206	206						
207	207						
208	208						
209	209						
210	210						
211	211						
212	212						
213	213						
214	214						
215	215						
216	216						
217	217						
218	218						
219	219						
220	220						
221	221						
222	222						
223	223						
224	224						
225	225						
226	226						
227	227						
228	228						
229	229						
230	230						
231	231						
232	232						
233	233						
234	234						
235	235						
236	236						
237	237						
238	238						
239	239						
240	240						
241	241						
242	242						
243	243						
244	244						
245	245						
246	246						
247	247						
248	248						
249	249						
250	250						

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TABLE X Critical values of  $F_{\max}$ 

$p \alpha$	2	3	4	5	6	7	8	9	10	11	12
2	39.0 199.	87.5 448.	142. 729.	202. 1036.	266. 1362.	333. 1705.	403. 2063.	475. 2432.	550. 2813.	626. 3204.	704. 3605.
3	15.4 47.5	27.8 85.	39.2 120.	50.7 151.	62.0 184.	72.9 21(6)	83.5 24(9)	93.9 28(1)	104. 31(0)	114. 33(7)	124. 36(1)
4	9.60 23.2	15.5 37.	20.6 49.	25.2 59.	29.5 69.	33.6 79.	37.5 89.	41.1 97.	44.6 106.	48.0 113.	51.4 120.
5	7.15 14.9	10.8 22.	13.7 28.	16.3 33.	18.7 38.	20.8 42.	22.9 46.	24.7 50.	26.5 54.	28.2 57.	29.9 60.
6	5.82 11.1	8.38 15.5	10.4 19.1	12.1 22.	13.7 25.	15.0 27.	16.3 30.	17.5 32.	18.6 34.	19.7 36.	20.7 37.
7	4.99 8.89	6.94 12.1	8.44 14.5	9.70 16.5	10.8 18.4	11.8 20.	12.7 22.	13.5 23.	14.3 24.	15.1 26.	15.8 27.
8	4.43 7.50	6.00 9.9	7.18 11.7	8.12 13.2	9.03 14.5	9.78 15.8	10.5 16.9	11.1 17.9	11.7 18.9	12.2 19.8	12.7 21.
9	4.03 6.54	5.34 8.5	6.31 9.9	7.11 11.1	7.80 12.1	8.41 13.1	8.95 13.9	9.45 14.7	9.91 15.3	10.3 16.0	10.7 16.6
10	3.72 5.85	4.85 7.4	5.67 8.6	6.34 9.6	6.92 10.4	7.42 11.1	7.87 11.8	8.28 12.4	8.66 12.9	9.01 13.4	9.34 13.9
12	3.28 4.91	4.16 6.1	4.79 6.9	5.30 7.6	5.72 8.2	6.09 8.7	6.42 9.1	6.72 9.5	7.00 9.9	7.25 10.2	7.48 10.6
15	2.86 4.07	3.54 4.9	4.01 5.5	4.37 6.0	4.68 6.4	4.95 6.7	5.19 7.1	5.40 7.3	5.59 7.5	5.77 7.8	5.98 8.0
20	2.46 3.32	2.95 3.8	3.29 4.3	3.54 4.6	3.76 4.9	3.94 5.1	4.10 5.3	4.24 5.5	4.37 5.6	4.49 5.8	4.59 5.9
30	2.07 2.63	2.40 3.0	2.61 3.3	2.78 3.4	2.91 3.6	3.02 3.7	3.12 3.8	3.21 3.9	3.29 4.0	3.36 4.1	3.39 4.2
60	1.67 1.96	1.85 2.2	1.96 2.3	2.04 2.4	2.11 2.4	2.17 2.5	2.22 2.5	2.26 2.6	2.30 2.6	2.33 2.7	2.36 2.7
$\infty$	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00	1.00 1.00

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